



KERALA AGRICULTURAL UNIVERSITY
B.Tech. (Agrl. Engg.) 2022 & Previous Admissions
II Semester Final Examination - September 2023

Sacs.1206

Engineering Mathematics - II (2+1)

Marks: 50
Time: 2 hours

I Choose the correct answer

(10x1=10)

- Series $1 + r + r^2 + \dots + \infty$ is
 - Converges if $|r| < 1$
 - diverges if $|r| < 1$
 - Oscillatory if $|r| < 1$
 - none of these
- The series $\sum u_n$ of positive terms is convergent or divergent as $\lim_{n \rightarrow \infty} \left[n \left(\frac{u_n}{u_{n+1}} - 1 \right) \right] > 1$ or < 1 , then this test is known as
 - Comparison test
 - Raabe's test
 - D-Alembert's ratio test
 - Cauchy's root test
- The Fourier series expansion of x in the interval $-1 \leq x \leq 1$ with periodic condition has
 - only sine terms
 - only cosine terms
 - both sine and cosine terms
 - only sine terms and a non-zero constant.
- The value of a_0 in the cosine series expansion of $f(x) = x$ in $(0,5)$ is
 - 2
 - 3
 - 5
 - 10
- Rational function $f(z) = \frac{3 + 2z + z^3}{4 + 5z + 3z^3}$ is
 - Analytic
 - Not analytic
 - Analytic only when $3 + 2z + z^3$ does not vanish
 - Analytic only when $4 + 5z + 3z^3$ does not vanish.
- The Fourier Cosine transform of $f(x) = \begin{cases} k, & \text{if } 0 < x < 1 \\ 0, & \text{if } x \geq 1 \end{cases}$ is
 - $k \sqrt{\frac{2}{\pi}} \frac{\sin s}{s}$
 - $\sqrt{\frac{2}{\pi}} \frac{\sin ks}{s}$
 - $k \sqrt{\frac{2}{\pi}} \frac{\cos s}{s}$
 - $\sqrt{\frac{2}{\pi}} \frac{\cos ks}{s}$

7. The Partial differential equation $\frac{\partial^2 u}{\partial t^2} = c^2 \frac{\partial^2 u}{\partial x^2}$, $c \neq 0$ is known as.....
- One dimensional heat equation
 - One dimensional wave equation
 - Laplace equation
 - None of these
8. The partial differential equation formed from the expression $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$ by eliminating arbitrary constants a and b is.....
- $2z = px + qy$
 - $2z = qx + py$
 - $z = px + qy$
 - $z = qx + py$
9. Analytic function with constant modulus is
- Constant
 - Need not be a constant
 - depends on the analytic function
 - None of these.

State True or False

10. "If $f(x)$ is non-periodic and defined in $(-\infty, \infty)$, the Fourier series expansion of $f(x)$ is not possible".

II Write short notes on ANY FIVE of the following

(5x2=10)

- Examine the convergence of $\sum_{k=1}^{\infty} \frac{4^k}{k^2}$
- Find the Fourier sine integral of $f(x) = \begin{cases} 1 & \text{if } 0 < x < \pi \\ 0 & \text{if } x > \pi \end{cases}$
- Find the half range sine series representation of $f(x) = k$ in $(0, \pi)$
- Form the partial differential equation by eliminating the arbitrary constants from $z = xy + y\sqrt{x+a} + b$
- Write down the possible solutions of one dimensional wave equation.
- Check whether the function $f(z) = e^x(\cos y - i \sin y)$ is analytic or not.
- Evaluate $\int_C \operatorname{Re}(z) dz$ where C is the shortest path from $1 + i$ to $5 + 5i$

III Answer ANY FIVE of the following

(5x4=20)

- Examine the convergence of $\sum_{k=1}^{\infty} (-1)^{k+1} e^{-k}$ using alternating series test.
- Test the convergence of $\sum_{k=1}^{\infty} \left(\frac{2k+1}{4k-3}\right)^k$
- Find the Fourier series of $f(x) = x$ in $-\pi < x < \pi$.
- Prove that an analytic function of constant real part is constant.
- Evaluate $\int_C \frac{1}{z^2+4} dz$ where C is $|z-2|=2$
- What type of singularity have the function $f(z) = e^{1/z}$
- Using the method of separation of variables, solve $\frac{\partial u}{\partial x} = 4 \frac{\partial u}{\partial y}$

IV Write an essay on ANY ONE of the following

(1x10=10)

- Solve $(mz - ny) \frac{\partial z}{\partial x} + (nx - lz) \frac{\partial z}{\partial y} = ly - mx$.
- Show that $v = (2x-1)y$ is harmonic and find the corresponding analytic function $f(z) = u(x, y) + iv(x, y)$.
