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KERALA AGRICULTURAL UNIVERSITY B.Tech.(Food Engg.) 2016 Admission III Semester Final Examination-Janauary-2018 Engineering Mathematics-III (2+1)

Marks: 50 Time: 2 hours (10x1=10)

Fill in the blanks:

1 Gradient of a scalar function is a scalar and the divergence of a constant is _____

Choose the Correct answer

2 $div(grad\phi) =$

a 0 👫 div(\$) c grad\$ d 🖈

3 If $\phi = 2x^3y^2z^4$ then $(\nabla^2\phi)_{(1,1,1)} =$

- a 24 b 12 c 40 d 36
- 4 If f(x) is an odd function defined in (-L,L), what is the value of a₀

- 5 A certain function u(x,y) can be the real part of an analytic function if
 - a u satisfies C-R equation c u is harmonic
 - b u is a continuous function d None of these
- ⁶ The value of the integral $\int_{C} \frac{dz}{z^2} = 0$ where C is,

a |z|=1 b |z-1|=2 c |z|=2 d |z-2|=1

State True or False

7 The vector function is the gradient of a scalar function, then the function is conservative

- 8 If $f(x)=1, 0 < x < \infty$ can be represent as a Fourier integral.
- 9 If f(z) is analytic function, then kf(z) is also analytic function where k is a constant.

Define the following

10 Write Parseval's identity for Fourier Sine Transform

Write Short notes on ANY FIVE of the following

1 Show that the function $\mathbf{x}^4 - 6\mathbf{x}^2\mathbf{y}^2 + \mathbf{y}^4$ is harmonic.

2 Verify whether w=sin(x)cosh(y)+icos(x)sinh(y) is analytic or not.

³ The Laurent's series expansion of $\frac{1}{z(z-1)}$ valid in |z| > 1 is

- 4 Find the Fourier cosine transform of e^{-x}.
- 5 Find the constant term in the Fourier series corresponding to f(x)=cos²(x) expressed in the interval (-π, π).
- 6 If $\vec{\mathbf{r}} = \mathbf{x}\vec{\mathbf{i}} + \mathbf{y}\vec{\mathbf{j}} + \mathbf{z}\vec{\mathbf{k}}$, then find $\nabla \left(\frac{1}{\mathbf{r}}\right)$?
- 7 If $\vec{\mathbf{F}} = (\mathbf{x} 3\mathbf{y})\vec{\mathbf{i}} + (\mathbf{y} 2\mathbf{x})\vec{\mathbf{j}}$ and C is the line segment from (0,0) to (3,1) then find $\int \vec{\mathbf{F}} d\vec{\mathbf{r}}$.

(5x2=10)

III

IV

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Answer ANY FIVE of the following

- Find the directional derivative of $\phi = xy + yz + zx$ in the direction of the vector $\vec{i} + 2\vec{j} + 2\vec{k}$ at (1,2,0).
- ² Evaluate $\int (\mathbf{x} d\mathbf{y} \mathbf{y} d\mathbf{x})$ around the circle $\mathbf{x}^2 + \mathbf{y}^2 = 1$.
- 3 Evaluate $\int \{(xy + x^2)dx + (x^2 + y^2)dy\}$, where C is the square formed by the lines x = -1 to 1 and y = -1 to lusing Green's theorem.

If for $0 \le x \le L$, the function f(x) has the expansion $f(x) = \sum_{n=1}^{\infty} b_n \sin(\frac{n\pi x}{L})$ then find $\int_{0}^{L} [f(x)]^2 dx$.

- 5 Find the Fourier Transform of $f(x) = \begin{cases} 1; & |x| < a \\ 0; & |x| > a \end{cases}$
- Find the Fourier transform of $e^{-|x|}$, then find $\int_{0}^{\infty} \frac{dx}{(x^2+1)^2}$.
- 7 Find the image of the circle |z|=2 by the transformation w=z+3+2i

Write an essay on ANY ONE of the following

(1x10=10)

(5x4=20)

- Evaluate $\int_{0}^{\infty} \frac{dx}{(x^2 + a^2)(x^2 + b^2)}$ using Fourier Transform.
- ² Use divergence theorem to evaluate $\iint_{S} \vec{F} \cdot \hat{n} ds$ where $\vec{F} = x^{3} \vec{i} + y^{3} \vec{j} + z^{3} \vec{k}$ and S is the surface of the sphere $x^{2} + y^{2} + z^{2} = a^{2}$.