# KERALA AGRICULTURAL UNIVERSITY 

## B. Tech.(Food Engg) 2016 Admission <br> IV Semester Final Examination-July 2018

Basc. 2209 Numerical Methods for Engineering Applications (1+1)
Marks: 50
Time:2hours

I Fill up the following blanks:
1 In $\qquad$ method the values of $\mathrm{x}_{1}, \mathrm{x}_{2}, \ldots \ldots \ldots, \mathrm{x}_{\mathrm{n}}$ are obtained immediately without using back substitution.
2 Lagrange's interpolation formula is used only for $\qquad$ intervals.
3 One dimensional heat equation is $\qquad$
4 The positive root of $f(x)=2 x^{3}-3 x-6=0$ lies between $\qquad$
5 Iterative formula of Newton's Raphson method is $\qquad$

## State True or False

6 Newton-Raphson method is quadratically convergent.
7 Solution matrix of $\mathrm{AX}=\mathrm{B}$ by Gauss-elimination method is an upper triangular matrix.
8 Newton's forward interpolation formula is suitable to estimate the interpolations near the middle of the table value.
9 Modified Euler's method is the Runge-Kutta method of fourth order.
10 Error in the trapezoidal rule is of the order $h^{4}$.

II Write Short notes on any FIVE of the following
1 Define interpolation and extrapolation.
2 i) Write trapezoidal rule.
ii) Write Newton's backward difference interpolation formula.

3 Classify the PDE $f_{X x}-2 f_{x y}=0$.
4 Using Gauss elimination method solve $2 \mathrm{x}+\mathrm{y}=3$

$$
7 x-3 y=4
$$

5 Find relation between E and $\Delta$
6 Form the divided difference table for the following data

| $x$ | 1 | 2 | 4 | 7 | 12 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $f(x)$ | 22 | 30 | 82 | 106 | 206 |

7
Evaluate $\int_{0}^{1}\left(\frac{1}{1+x^{2}}\right) \mathrm{dx}$ using Trapezoidal rule by taking interval $\mathrm{h}=\frac{1}{2}$

III Answer any FIVE of the following.
(5x4=20)
1 Solve the equation $x^{3}-2 x-5=0$ by Newton Raphson method.
2 Using Newton's forward interpolation formula find y at $x=8$ from the table:

| $x$ | 0 | 5 | 10 | 15 | 20 | 25 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 7 | 11 | 14 | 18 | 24 | 32 |

3 Find the value of $\int_{1}^{2}\left(\frac{1}{5+3 x}\right) \mathrm{dx}$ using Simpson's rule.
4 Obtain the values of $y$ at $x=0.1,0.2$ using R.K method of second order.
5 Solve $\frac{d y}{d x}=x+y$, given $y(1)=0$, and get $y(1.1)$ by Taylor series method.
6 Using Crank-Nicholson's method solve $\mathrm{u}_{\mathrm{Xx}}=16 \mathrm{u}_{\mathrm{t}}, 0<\mathrm{x}<1, \mathrm{t}>0$ given $\mathrm{u}(\mathrm{x}, 0)=0, \mathrm{u}(0, \mathrm{t})=0, \mathrm{u}(1, \mathrm{t})=100 \mathrm{t}$. Compute u for one step in $t$ direction taking $\mathrm{h}=\frac{1}{4}$.
7 Write short notes on classification of partial differential equation of second order.

## IV Write Essay on ANY ONE

$(1 \times 10=10)$

1. Explain briefly Gauss elimination and Gauss Jordan Methods.
2. The following are data from steam table.

| Temp ${ }^{\circ} \mathrm{C}$ | 140 | 150 | 160 | 170 | 180 |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Pressure $\mathrm{Kg} / \mathrm{cm}^{2}$ | 3.685 | 4.854 | 6.302 | 8.076 | 10.225 |

Using Newton's formula, find the pressure of the steam for a temperature of $142^{\circ} \mathrm{C}$.

